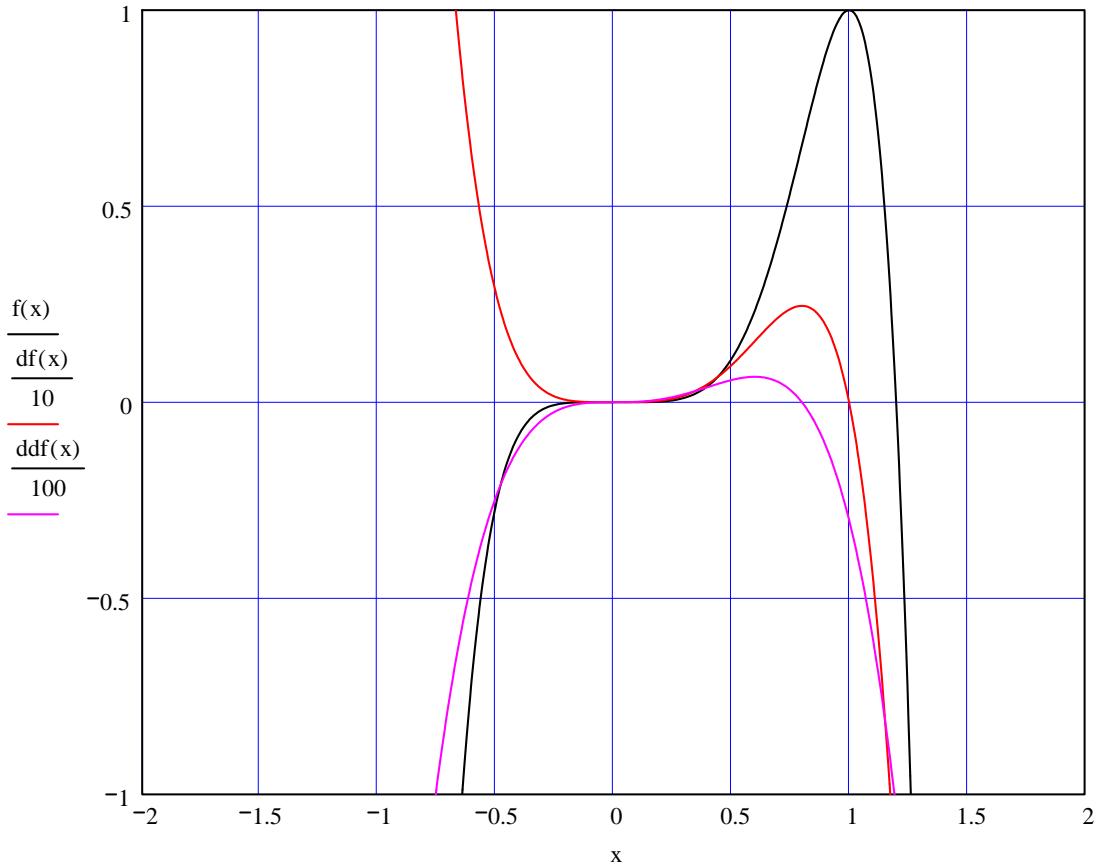


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D2(1)

$$f(x) := 6 \cdot x^5 - 5 \cdot x^6 \quad df(x) := \frac{d}{dx} f(x) \quad ddfa(x) := \frac{d}{dx} df(x) \quad ddf(x) := \frac{d^2}{dx^2} f(x)$$

$$df(x) \rightarrow 30 \cdot x^4 - 30 \cdot x^5 \quad ddf(x) \rightarrow 120 \cdot x^3 - 150 \cdot x^4$$



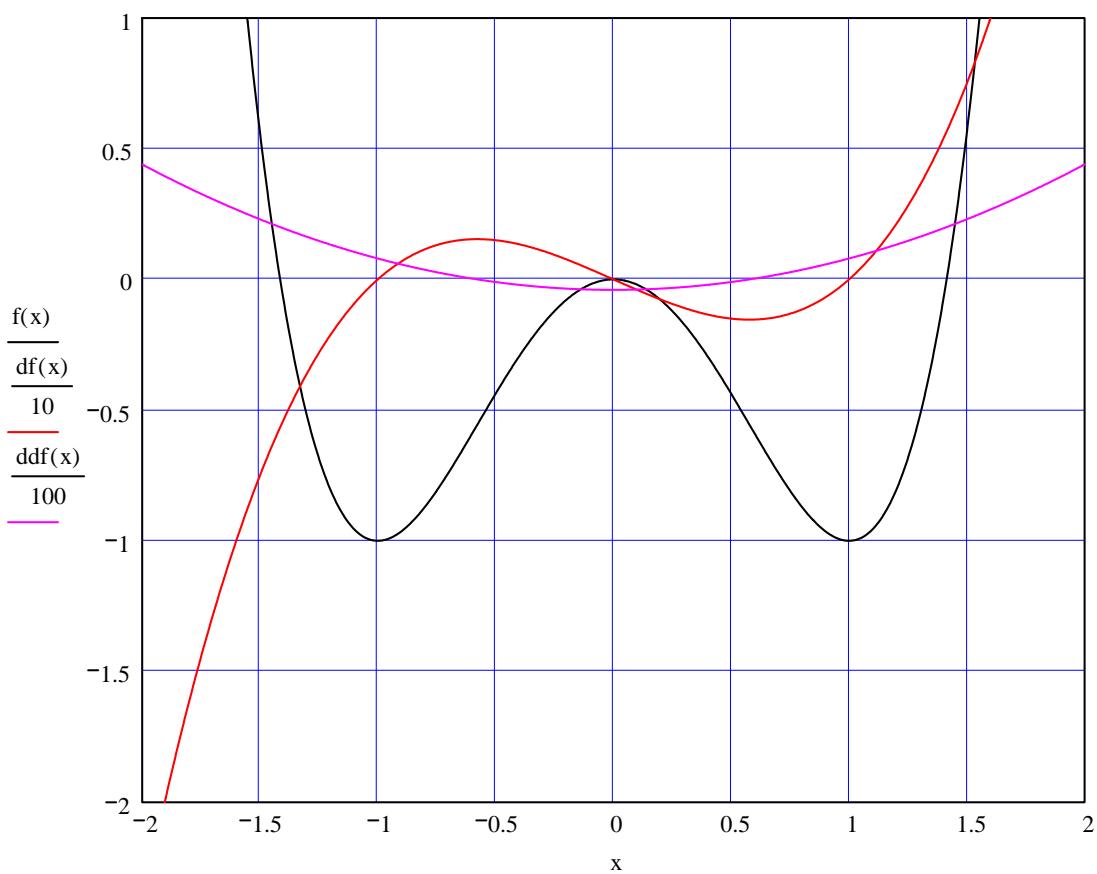
Given $df(x) = 0$ Find(x) $\rightarrow (0 \ 0 \ 0 \ 0 \ 1)$

$xa := 0$ $ddf(xa) \rightarrow 0$ $xb := 1$ $ddf(xb) \rightarrow -30$

D2(2)

$$f(x) := x^4 - 2 \cdot x^2 \quad df(x) := \frac{d}{dx} f(x) \quad ddfa(x) := \frac{d}{dx} df(x) \quad ddf(x) := \frac{d^2}{dx^2} f(x)$$

$$df(x) \rightarrow 4 \cdot x^3 - 4 \cdot x \quad ddf(x) \rightarrow 12 \cdot x^2 - 4$$



Given $df(x) = 0$ Find(x) $\rightarrow (0 \ 1 \ -1)$

$$xa := 0 \quad ddf(xa) \rightarrow -4$$

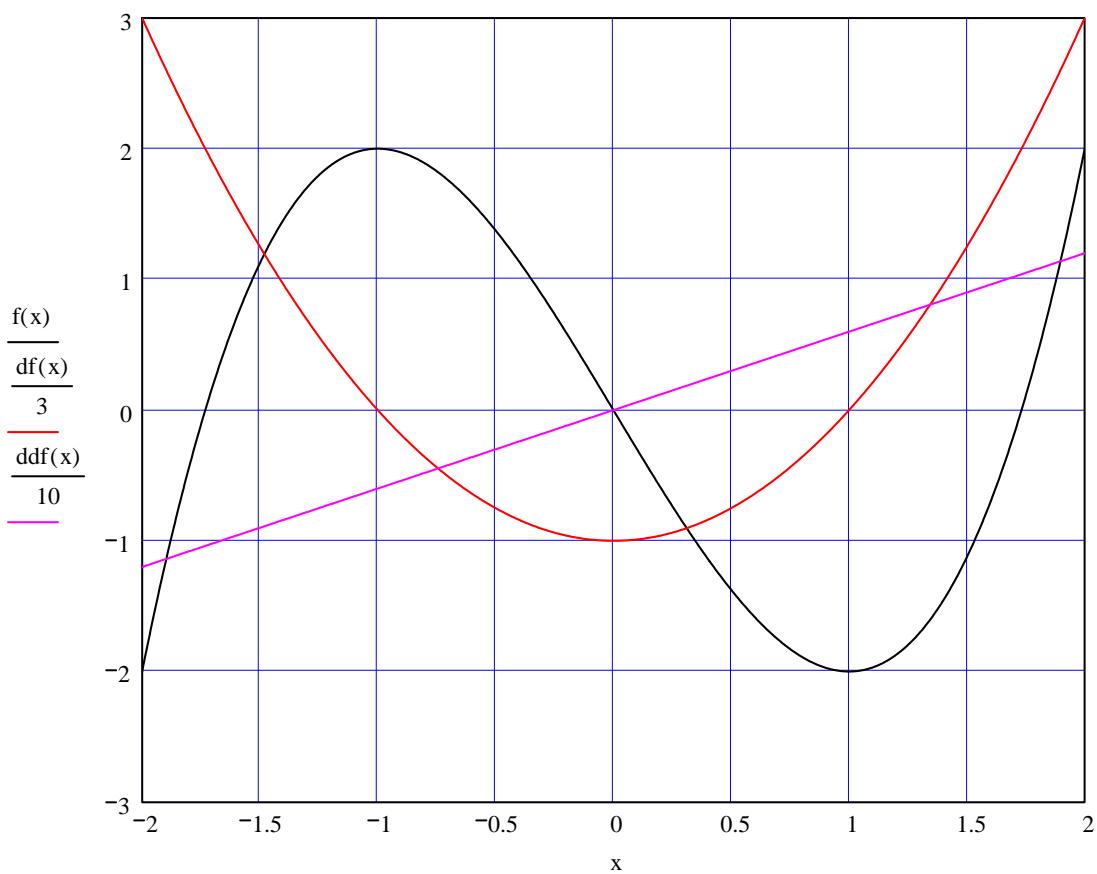
$$xb := 1 \quad ddf(xb) \rightarrow 8$$

$$xc := -1 \quad ddf(xb) \rightarrow 8$$

D2(3)

$$f(x) := x^3 - 3 \cdot x \quad df(x) := \frac{d}{dx} f(x) \quad ddfa(x) := \frac{d}{dx} df(x) \quad ddf(x) := \frac{d^2}{dx^2} f(x)$$

$$df(x) \rightarrow 3 \cdot x^2 - 3 \quad ddf(x) \rightarrow 6 \cdot x$$



Given $df(x) = 0$ Find($x \rightarrow (1 \ -1)$)

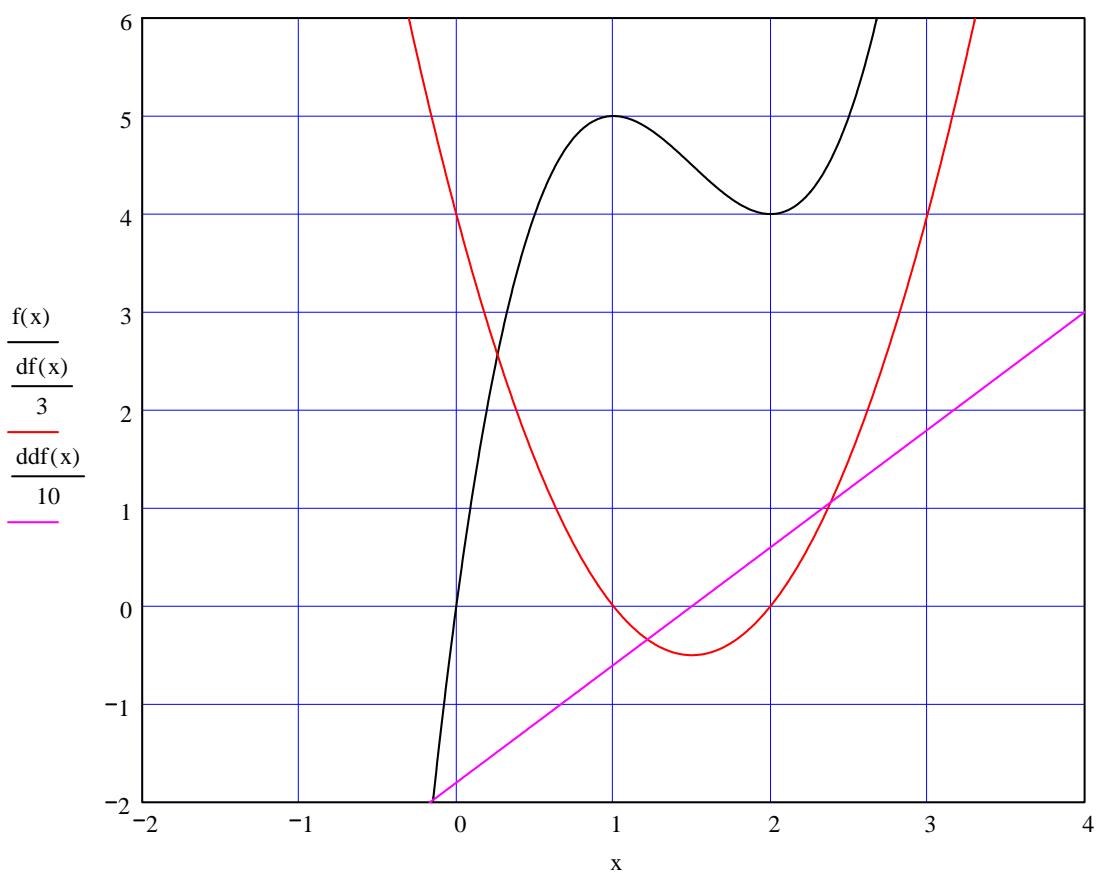
$xa := -1 \quad ddf(xa) \rightarrow -6$

$xb := 1 \quad ddf(xb) \rightarrow 6$

D2(5)

$$f(x) := 2x^3 - 9 \cdot x^2 + 12x \quad df(x) := \frac{d}{dx} f(x) \quad ddfa(x) := \frac{d}{dx} df(x) \quad ddf(x) := \frac{d^2}{dx^2} f(x)$$

$$df(x) \rightarrow 6 \cdot x^2 - 18 \cdot x + 12 \quad ddf(x) \rightarrow 12 \cdot x - 18$$



Given $df(x) = 0$ Find(x) $\rightarrow (1 \ 2)$

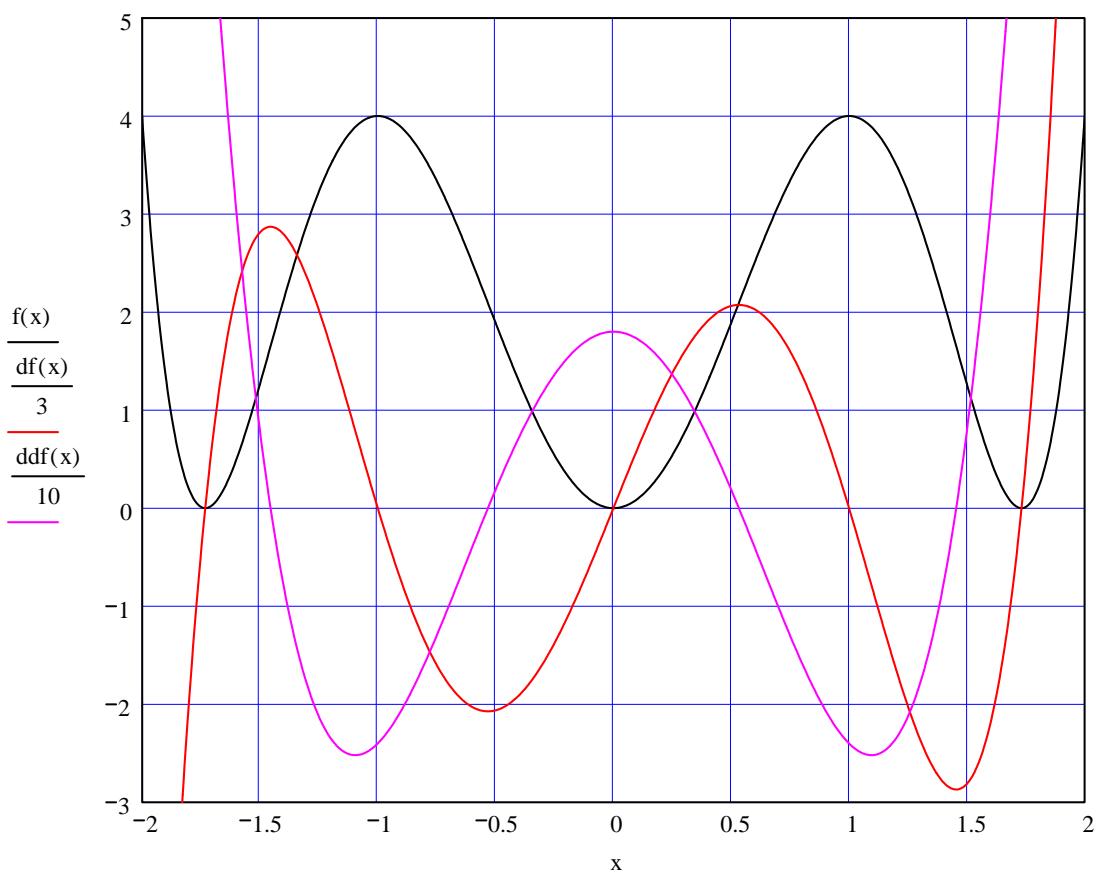
$xa := 1$ $ddf(xa) \rightarrow -6$

$xb := 2$ $ddf(xb) \rightarrow 6$

D2(6)

$$f(x) := x^6 - 6 \cdot x^4 + 9x^2 \quad df(x) := \frac{d}{dx} f(x) \quad ddf(x) := \frac{d^2}{dx^2} f(x)$$

$$df(x) \rightarrow 6 \cdot x^5 - 24 \cdot x^3 + 18 \cdot x \quad ddf(x) \rightarrow 30 \cdot x^4 - 72 \cdot x^2 + 18$$



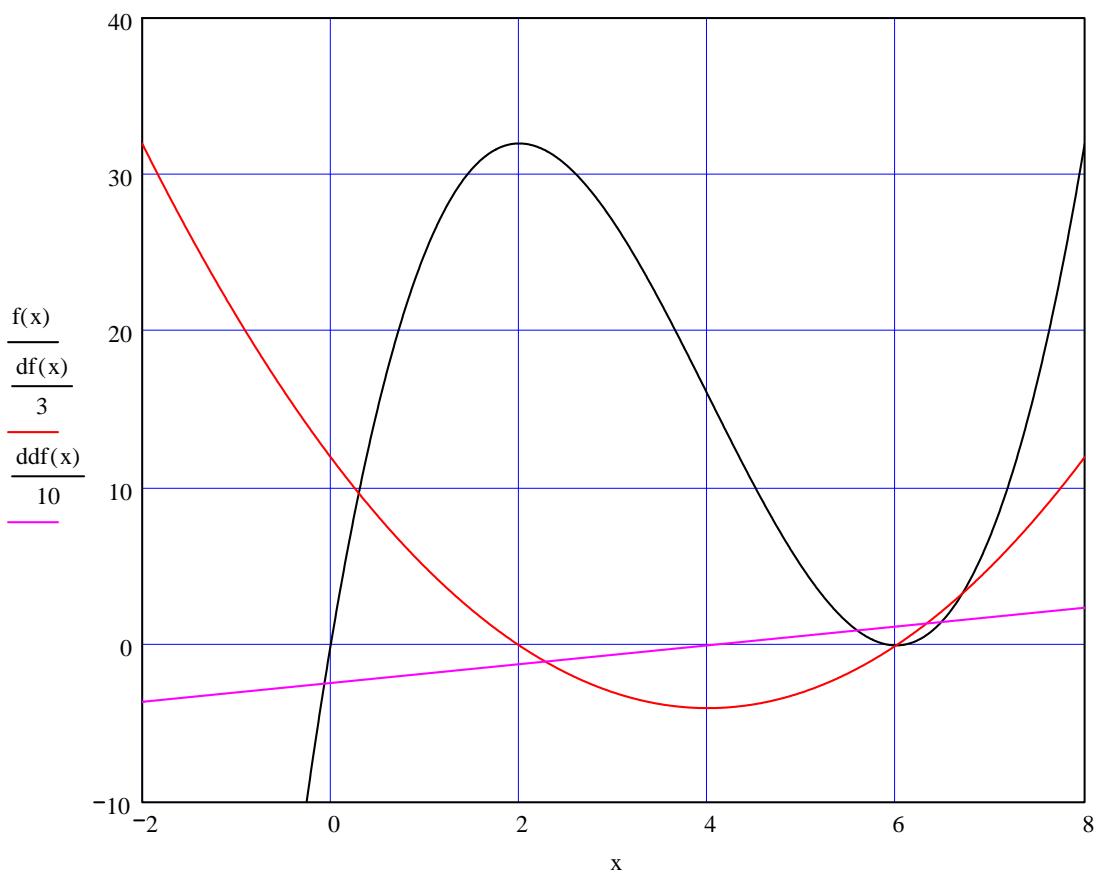
Given $df(x) = 0$ Find(x) $\rightarrow \begin{pmatrix} & & \frac{1}{2} & \frac{1}{2} \\ 0 & 1 & -1 & 3^{\frac{1}{2}} & -3^{\frac{1}{2}} \end{pmatrix}$

| | | | |
|------------|---------------------------|-------------------|--------------------------|
| $xb := 1$ | $ddf(xb) \rightarrow -24$ | | |
| $xb := -1$ | $ddf(xb) \rightarrow -24$ | $xm := -\sqrt{3}$ | $ddf(xm) \rightarrow 72$ |
| $xc := 1$ | $ddf(xc) \rightarrow -24$ | $xn := \sqrt{3}$ | $ddf(xn) \rightarrow 72$ |

D2(7)

$$f(x) := x \cdot (6 - x)^2 \quad df(x) := \frac{d}{dx} f(x) \quad ddf(x) := \frac{d^2}{dx^2} f(x)$$

$$df(x) \rightarrow (6 - x)^2 - 2 \cdot x \cdot (6 - x) \quad ddf(x) \rightarrow 6 \cdot x - 24$$



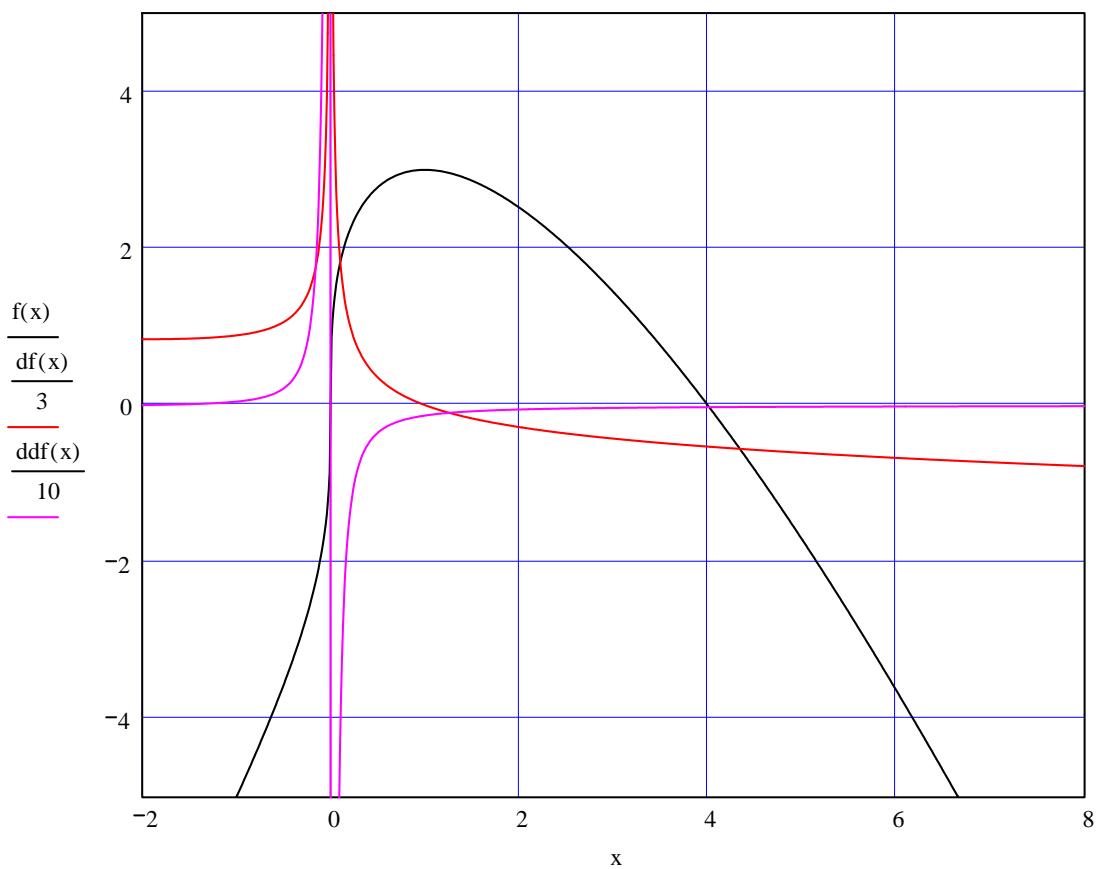
Given $df(x) = 0$ Find($x \rightarrow (2 \ 6)$)

$$xa := 2 \quad ddf(xa) \rightarrow -12$$

$$xb := 6 \quad ddf(xb) \rightarrow 12$$

D2(10)

$$\begin{aligned}
 f(x) &:= (4-x)\sqrt[3]{x} & df(x) &:= \frac{d}{dx}f(x) & ddf(x) &:= \frac{d^2}{dx^2}f(x) \\
 df(x) &\rightarrow -x^{\frac{1}{3}} + \frac{1}{3} \cdot \frac{4-x}{x^{\frac{2}{3}}} & ddf(x) &\rightarrow \frac{-2}{3x^{\frac{2}{3}}} - \frac{2}{9} \cdot \frac{4-x}{x^{\frac{5}{3}}}
 \end{aligned}$$



Given $df(x) = 0$ Find($x \rightarrow 1$)

$$xa := 1 \quad ddf(xa) \rightarrow \frac{-4}{3}$$