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for home

1 -st kind

direct computation

$$\int_1^{\infty} x^{-\frac{1}{3}} dx \rightarrow \infty \quad \int_1^{\infty} x^{-\frac{4}{3}} dx \rightarrow 3$$
$$\int_1^{\infty} x^{-\frac{5}{4}} dx \rightarrow 4 \quad \int_1^{\infty} x^{-\frac{5}{2}} dx \rightarrow \frac{2}{3} \quad \int_1^{\infty} x^{-2008} dx \rightarrow \frac{1}{2007} \quad \int_1^{\infty} x^{-\frac{2008}{2007}} dx \rightarrow 2007$$

by parts

$$\int_1^{\infty} x^{-3} \cdot \ln(x) dx \rightarrow \frac{1}{4} \quad \int_1^{\infty} x^{-3} \cdot \ln(x)^2 dx \rightarrow \frac{1}{4} \quad \int_1^{\infty} x^{-3} \cdot \ln(x)^3 dx \rightarrow \frac{3}{8} \quad \int_1^{\infty} x^{-3} \cdot \ln(x)^4 dx \rightarrow \frac{3}{4}$$
$$\int_1^{\infty} x^{-5} \cdot \ln(x) dx \rightarrow \frac{1}{16} \quad \int_1^{\infty} x^{-5} \cdot \ln(x)^2 dx \rightarrow \frac{1}{32} \quad \int_1^{\infty} x^{-5} \cdot \ln(x)^3 dx \rightarrow \frac{3}{128} \quad \int_1^{\infty} x^{-5} \cdot \ln(x)^4 dx \rightarrow \frac{3}{128}$$
$$\int_0^{\infty} x \cdot e^{-2x} dx \rightarrow \frac{1}{4} \quad \int_0^{\infty} x^2 \cdot e^{-2x} dx \rightarrow \frac{1}{4} \quad \int_0^{\infty} x^3 \cdot e^{-2x} dx \rightarrow \frac{3}{8} \quad \int_0^{\infty} x^4 \cdot e^{-2x} dx \rightarrow \frac{3}{4}$$

direct

$$\int_0^{\infty} \frac{1}{\frac{1}{4} + x^2} dx \rightarrow \pi \quad \int_0^{\infty} \frac{1}{9 + x^2} dx \rightarrow \frac{1}{6} \cdot \pi \quad \int_0^{\infty} \frac{x^2}{1 + x^6} dx \rightarrow \frac{1}{6} \cdot \pi$$

by parts

$$\int_0^{\infty} \frac{1}{(4 + x^2)^2} dx \rightarrow \frac{1}{32} \cdot \pi \quad \int_0^{\infty} \frac{1}{(4 + x^2)^3} dx \rightarrow \frac{3}{512} \cdot \pi$$
$$\int_0^{\infty} e^{-2x} \cdot \sin(x) dx \rightarrow \frac{1}{5} \quad \int_0^{\infty} e^{-2x} \cdot \cos(x) dx \rightarrow \frac{2}{5}$$
$$\int_1^{10000} \frac{\cos(\ln(x))}{x^2} dx \rightarrow \frac{1}{20000} \cdot \frac{-1 + \tan(2 \cdot \ln(2) + 2 \cdot \ln(5))^2 + 2 \cdot \tan(2 \cdot \ln(2) + 2 \cdot \ln(5))}{1 + \tan(2 \cdot \ln(2) + 2 \cdot \ln(5))^2} + \frac{1}{2} = 0.500059494708039$$

$$\int_1^{10000} \frac{\cos(\ln(x))}{x^4} dx \rightarrow \frac{1}{10000000000000} \cdot \frac{-3 + 2 \cdot \tan(2 \cdot \ln(2) + 2 \cdot \ln(5)) + 3 \cdot \tan(2 \cdot \ln(2) + 2 \cdot \ln(5))^2}{1 + \tan(2 \cdot \ln(2) + 2 \cdot \ln(5))^2} + \frac{3}{10} = 0.300000000$$

split to simple fractions and compute antiderivative

$$\int_0^{\infty} \frac{1}{x^2 + 6x + 5} dx \rightarrow \frac{1}{4} \cdot \ln(5) \quad \int_0^{\infty} \frac{1}{(x+1) \cdot (x+3) \cdot (x+5)} dx \rightarrow \frac{1}{4} \cdot \ln(3) - \frac{1}{8} \cdot \ln(5)$$

change variable

$$\int_0^{\infty} \frac{-x^2}{x \cdot e^{\frac{x^2}{2}}} dx \rightarrow 1$$

$$\int_0^{\infty} \frac{-x^2}{x \cdot e^{\frac{x^2}{2}}} dx \rightarrow 1 \quad \int_0^{\infty} x^{17} \cdot e^{-x^3} dx \rightarrow 40 \quad \int_0^{\infty} x^7 \cdot e^{-x^4} dx \rightarrow \frac{1}{4}$$

$$\int_0^{\infty} x^5 \cdot e^{-x^2} dx \rightarrow 1 \quad \int_0^{\infty} x^{11} \cdot e^{-x^3} dx \rightarrow 2 \quad \int_0^{\infty} x^{13} \cdot e^{-x^7} dx \rightarrow \frac{1}{7}$$

Let Known

$$\int_0^{\infty} e^{-\frac{x^2}{2}} dx \rightarrow \frac{1}{2} \cdot 2^{\frac{1}{2}} \cdot \pi^{\frac{1}{2}} \quad \int_{-\infty}^{\infty} e^{-\frac{x^2}{2}} dx \rightarrow 2^{\frac{1}{2}} \cdot \pi^{\frac{1}{2}}$$

by parts

$$\int_0^{\infty} \frac{-x^2}{x^2 \cdot e^{\frac{x^2}{2}}} dx \rightarrow \frac{1}{2} \cdot 2^{\frac{1}{2}} \cdot \pi^{\frac{1}{2}} \quad \int_0^{\infty} \frac{-x^2}{x^4 \cdot e^{\frac{x^2}{2}}} dx \rightarrow \frac{3}{2} \cdot 2^{\frac{1}{2}} \cdot \pi^{\frac{1}{2}} \quad \int_0^{\infty} \frac{-x^2}{x^6 \cdot e^{\frac{x^2}{2}}} dx \rightarrow \frac{15}{2} \cdot 2^{\frac{1}{2}} \cdot \pi^{\frac{1}{2}}$$

$$\int_0^{\infty} \frac{-x^6}{x^2 \cdot e^{\frac{x^2}{2}}} dx \rightarrow \frac{1}{6} \cdot 2^{\frac{1}{2}} \cdot \pi^{\frac{1}{2}} \quad \int_0^{\infty} \frac{-x^8}{x^3 \cdot e^{\frac{x^2}{2}}} dx \rightarrow \frac{1}{8} \cdot 2^{\frac{1}{2}} \cdot \pi^{\frac{1}{2}}$$

2 -nd kind

direct

$$\int_0^1 x^{-\frac{1}{3}} dx \rightarrow \frac{3}{2} \quad \int_0^1 x^{-\frac{5}{4}} dx \rightarrow \infty \quad \int_0^1 \frac{1}{\sqrt[3]{1-x}} dx \rightarrow \frac{3}{2} \quad \int_0^1 \frac{x}{\sqrt[3]{1-x}} dx \rightarrow \frac{9}{10}$$

by parts

$$\int_0^1 \ln(x)^2 dx \rightarrow 2 \quad \int_0^1 x \cdot \ln(x)^2 dx \rightarrow \frac{1}{4} \quad \int_0^1 x^2 \cdot \ln(x)^2 dx \rightarrow \frac{2}{27} \quad \int_0^1 x^3 \cdot \ln(x)^2 dx \rightarrow \frac{1}{32}$$

direct

$$\int_0^{\frac{1}{2}} \frac{1}{\sqrt{1-x^2}} dx \rightarrow \frac{1}{6} \cdot \pi$$

change variable

$$\int_{\frac{3}{5}}^{\frac{4}{5}} \frac{x}{\sqrt{1-x^2}} dx \rightarrow \frac{1}{5}$$

$$\int_0^{\frac{1}{2}} \frac{x^2}{\sqrt{1-x^2}} dx \rightarrow \frac{-1}{8} \cdot 3^{\frac{1}{2}} + \frac{1}{12} \cdot \pi$$

$$\int_0^{\frac{1}{2}} \frac{x^3}{\sqrt{1-x^2}} dx \rightarrow \frac{-3}{8} \cdot 3^{\frac{1}{2}} + \frac{2}{3}$$

$$\int_0^{\frac{1}{\sqrt{2}}} \frac{x}{\sqrt{1-x^4}} dx \rightarrow \frac{1}{12} \cdot \pi$$

$$\int_0^1 \frac{x^5}{\sqrt{1-x^4}} dx \rightarrow \frac{1}{8} \cdot \pi$$

$$\int_0^{\frac{1}{2}} \frac{1}{\sqrt{x-x^2}} dx \rightarrow \frac{1}{2} \cdot \pi$$

$$\int_0^{\frac{\pi}{2}} \sin(x) \cdot \ln(\cos(x)) dx \rightarrow -1$$

$$\int_0^{\frac{\pi}{2}} \sin(x)^3 \cdot \ln(\cos(x)) dx \rightarrow \frac{-8}{9}$$

$$\int_0^{\frac{\pi}{2}} \sin(x) \cdot \cos(x) \cdot \ln(\cos(x)) dx \rightarrow \frac{-1}{4}$$

$$\int_0^{\frac{\pi}{2}} \sin(x) \cdot \cos(x)^2 \cdot \ln(\cos(x)) dx \rightarrow \frac{-1}{9}$$

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