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for home

$$\int_0^5 x \cdot (5 - x) dx \rightarrow \frac{125}{6} \quad \int_0^3 x^2 \cdot (3 - x)^3 dx \rightarrow \frac{243}{20} \quad \int_0^2 x^2 \cdot (2 - x)^5 dx \rightarrow \frac{32}{21}$$

$$\int_1^2 \frac{1}{9 - x^2} dx \rightarrow \frac{1}{6} \cdot \ln(5) - \frac{1}{6} \cdot \ln(2) \quad \int_1^2 \frac{x}{9 - x^2} dx \rightarrow \frac{-1}{2} \cdot \ln(5) + \frac{3}{2} \cdot \ln(2)$$

$$\int_3^4 \frac{1}{x^2 - 8x + 12} dx \rightarrow \frac{-1}{4} \cdot \ln(3) \quad \int_3^4 \frac{x}{x^2 - 8x + 12} dx \rightarrow \ln(2) - \frac{3}{2} \cdot \ln(3)$$

$$\int_3^4 \frac{x^2}{x^2 - 8x + 12} dx \rightarrow 1 + 8 \cdot \ln(2) - 9 \cdot \ln(3)$$

$$\int_1^2 \frac{1}{x + 2} dx \rightarrow 2 \cdot \ln(2) - \ln(3) \quad \int_1^2 \frac{1}{x^2 + 4x + 4} dx \rightarrow \frac{1}{12} \quad \int_{-1}^1 \frac{1}{x^3 + 6x^2 + 12x + 8} dx \rightarrow \frac{4}{9}$$

$$\int_0^2 \frac{1}{x^2 + 4} dx \rightarrow \frac{1}{8} \cdot \pi \quad \int_{\frac{1}{2}}^{\frac{\sqrt{3}}{2}} \frac{1}{\sqrt{1 - x^2}} dx \rightarrow \frac{1}{6} \cdot \pi$$

$$\int_0^2 \frac{x}{x^2 + 4} dx \rightarrow \frac{1}{2} \cdot \ln(2) \quad \int_0^{\frac{1}{2}} \frac{x}{\sqrt{2 - x^2}} dx \rightarrow \frac{-1}{2} \cdot 7^{\frac{1}{2}} + 2^{\frac{1}{2}}$$

$$\int_0^1 \frac{1}{x^2 - x + 1} dx \rightarrow \frac{2}{9} \cdot 3^{\frac{1}{2}} \cdot \pi \quad \int_0^1 \frac{x}{x^2 - x + 1} dx \rightarrow \frac{1}{9} \cdot 3^{\frac{1}{2}} \cdot \pi$$

$$\int_0^\pi \sin(3x) dx \rightarrow \frac{2}{3} \quad \int_0^{\frac{\pi}{2}} \cos(3x) dx \rightarrow \frac{-1}{3}$$

$$\int_0^{\frac{\pi}{2}} \cos(x)^2 dx \rightarrow \frac{1}{4} \cdot \pi \quad \int_0^{\frac{\pi}{2}} \sin(x) \cdot \cos(x)^5 dx \rightarrow \frac{1}{6} \quad \int_0^{\frac{\pi}{2}} \cos(x)^3 \cdot \sin(x)^4 dx \rightarrow \frac{2}{35}$$

$$\int_0^{\frac{\pi}{2}} \sin(x) \cdot \cos(x)^{123} dx \rightarrow \frac{1}{124} \quad \int_0^{\frac{\pi}{2}} \sin(x)^3 \cdot \cos(x)^2 dx \rightarrow \frac{2}{15} \quad \int_0^{\frac{\pi}{2}} \cos(x)^4 \cdot \sin(x)^4 dx \rightarrow \frac{3}{256} \cdot \pi$$

$$\int_{\frac{\pi}{6}}^{\frac{\pi}{4}} \frac{1}{\cos(x)^2} dx \rightarrow 1 - \frac{1}{3} \cdot 3^{\frac{1}{2}}$$

$$\int_{\frac{\pi}{6}}^{\frac{\pi}{4}} \frac{1}{\cos(x)} dx \rightarrow \ln\left(2^{\frac{1}{2}} + 1\right) - \frac{1}{2} \cdot \ln(3)$$

$$\int_0^{\pi} x \cdot \cos(x) dx \rightarrow -2 \quad \int_0^{\pi} x^2 \cdot \cos(x) dx \rightarrow -2 \cdot \pi$$

$$\int_0^1 x \cdot e^{-x} dx \rightarrow -2 \cdot \exp(-1) + 1 \quad \int_0^1 x^2 \cdot e^{-x} dx \rightarrow -5 \cdot \exp(-1) + 2 \quad \int_0^1 x^3 \cdot e^{-x} dx \rightarrow -16 \cdot \exp(-1) + 6$$

$$\int_0^{\pi} \sin(x) \cdot e^{-x} dx \rightarrow \frac{1}{2} \cdot \exp(-\pi) + \frac{1}{2} \quad \int_{-\pi}^{\pi} \cos(x) \cdot e^{-3x} dx \rightarrow \frac{3}{10} \cdot \exp(-3 \cdot \pi) - \frac{3}{10} \cdot \exp(3 \cdot \pi)$$

$$\int_1^e \cos(\ln(x)) dx \rightarrow \frac{1}{2} \cdot \sin(1) \cdot \exp(1) + \frac{1}{2} \cdot \exp(1) \cdot \cos(1) - \frac{1}{2}$$

$$\int_0^{\sqrt[3]{\pi}} x^2 \cdot \sin(x^3) dx \rightarrow \frac{2}{3} \quad \int_1^2 x^4 \cdot \ln(x^5) dx \rightarrow 32 \cdot \ln(2) - \frac{31}{5}$$

$$\int_1^2 x \cdot \sin(x^2) \cdot e^{x^2} dx \rightarrow \frac{-1}{4} \cdot \exp(4) \cdot \cos(4) + \frac{1}{4} \cdot \sin(4) \cdot \exp(4) + \frac{1}{4} \cdot \exp(1) \cdot \cos(1) - \frac{1}{4} \cdot \sin(1) \cdot \exp(1)$$

$$\int_{\frac{-1}{\sqrt{3}}}^1 \operatorname{atan}(x) dx \rightarrow \frac{1}{4} \cdot \pi + \frac{1}{2} \cdot \ln(2) - \frac{1}{18} \cdot 3^{\frac{1}{2}} \cdot \pi - \frac{1}{2} \cdot \ln(3) \quad \int_{\frac{-1}{\sqrt{3}}}^1 x \cdot \operatorname{atan}(x) dx \rightarrow \frac{13}{36} \cdot \pi - \frac{1}{2} - \frac{1}{6} \cdot 3^{\frac{1}{2}}$$

$$\int_{\frac{1}{\sqrt{3}}}^{\sqrt{3}} \frac{\sqrt{\operatorname{atan}(x)}}{1+x^2} dx \rightarrow \frac{2}{27} \cdot 3^{\frac{1}{2}} \cdot \pi^{\frac{3}{2}} - \frac{1}{54} \cdot 6^{\frac{1}{2}} \cdot \pi^{\frac{3}{2}} \quad \int_{\frac{1}{\sqrt{3}}}^{\sqrt{3}} \frac{x \cdot \operatorname{atan}(x^2)}{1+x^4} dx \rightarrow \frac{1}{4} \cdot \operatorname{atan}(3)^2 - \frac{1}{4} \cdot \operatorname{atan}\left(\frac{1}{3}\right)^2$$

$$\int_{\frac{1}{3}}^3 \frac{\cos(x) \cdot \operatorname{atan}(\sin(x))}{(1+\sin(x)^2)} dx \rightarrow \frac{1}{2} \cdot \operatorname{atan}(\sin(3))^2 - \frac{1}{2} \cdot \operatorname{atan}\left(\sin\left(\frac{1}{3}\right)\right)^2$$

$$\int_{\frac{1}{\sqrt{2}}}^1 \operatorname{asin}(x) dx \rightarrow \frac{1}{2} \cdot \pi - \frac{1}{8} \cdot 2^{\frac{1}{2}} \cdot \pi - \frac{1}{2} \cdot 2^{\frac{1}{2}} \quad \int_{\frac{1}{\sqrt{2}}}^1 x \cdot \operatorname{asin}(x) dx \rightarrow \frac{1}{8} \cdot \pi - \frac{1}{8}$$

$$\int_{\frac{1}{2}}^{\sqrt{3}} \frac{\operatorname{asin}(x)^2}{\sqrt{1-x^2}} dx \rightarrow \frac{7}{648} \cdot \pi^3 \quad \int_0^3 \frac{x \cdot \operatorname{asin}(x^2)}{\sqrt{1-x^4}} dx \rightarrow \frac{1}{4} \cdot \operatorname{asin}\left(\frac{9}{16}\right)^2$$

die hard $\int_0^1 x \cdot \ln(x)^2 dx \rightarrow \frac{1}{4} \quad \int_0^1 x^2 \cdot \ln(x)^2 dx \rightarrow \frac{2}{27} \quad \int_0^1 x^3 \cdot \ln(x)^2 dx \rightarrow \frac{1}{32}$

$$\int_1^e x \cdot \ln(x)^2 dx \rightarrow \frac{1}{4} \cdot \exp(2) - \frac{1}{4} \quad \int_1^e x^2 \cdot \ln(x)^2 dx \rightarrow \frac{5}{27} \cdot \exp(3) - \frac{2}{27}$$